

Seamless phase 2/3 design with benefit-risk driven treatment selection using multi-criteria decision analysis (MCDA)

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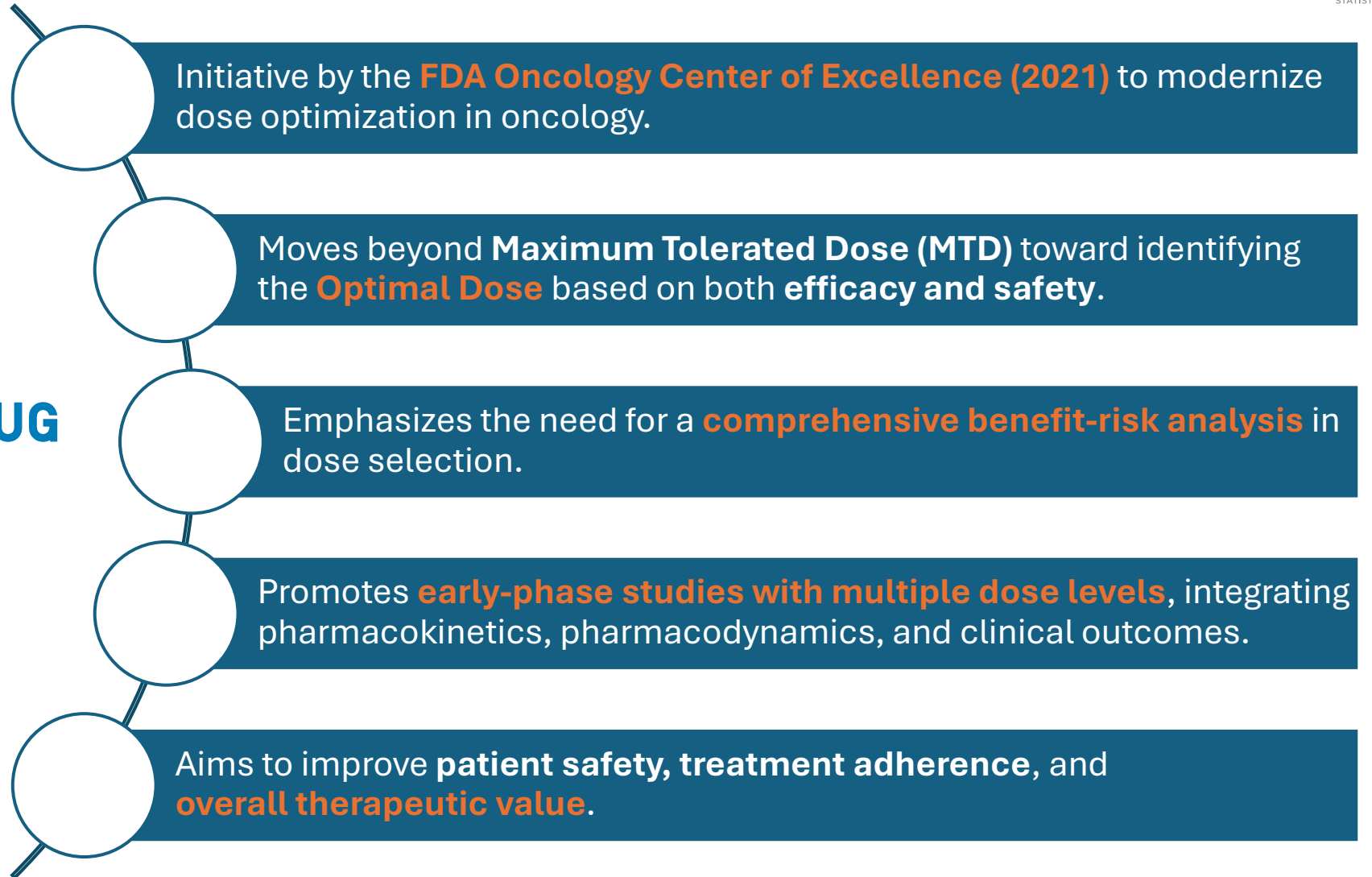
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FDA project Optimus



Trial design

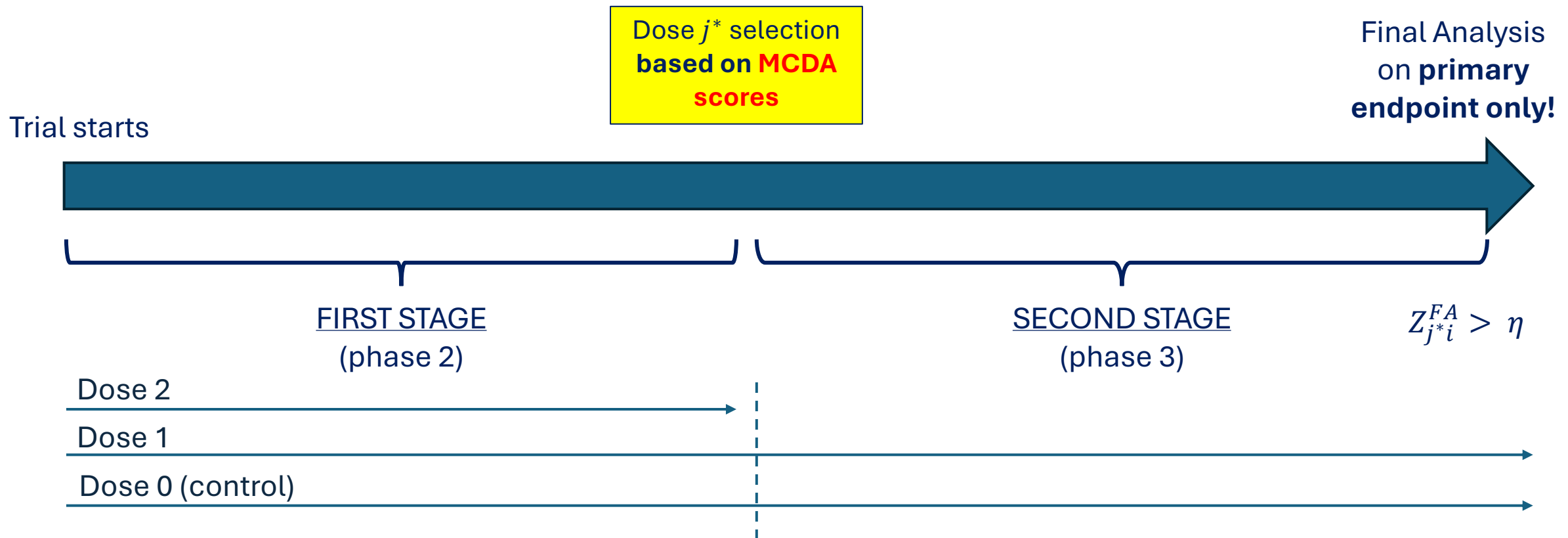
$j = 0, 1, 2, \dots, J$: index of the dose ($j = 0$ is the control arm)

$i = 1, 2, \dots, I$: index of safety/efficacy endpoints ($i = 1$ is the primary efficacy endpoint)

θ_{ji} : j -th parameter of interest for the i -th dose

δ_{ji} : treatment difference in the i -th endpoint related to the j -th dose

Z_{ji}^* : Test statistic for the i -th endpoint related to the j -th dose at the time point $\star = IA, FA$



Structure of the parameters MLEs

For each dose j the maximum likelihood estimators of the parameters of interest are supposed to follow a multivariate normal distribution

$$\begin{pmatrix} \hat{\theta}_{j1} \\ \vdots \\ \hat{\theta}_{jI} \end{pmatrix} = \text{Normal} \left(\begin{pmatrix} \theta_{j1} \\ \vdots \\ \theta_{jI} \end{pmatrix}, \begin{pmatrix} \sigma_{j1}^2 & \cdots & \rho_{1I}\sigma_{j1}\sigma_{jI} \\ \vdots & \ddots & \vdots \\ \rho_{1I}\sigma_{j1}\sigma_{jI} & \cdots & \sigma_{jI}^2 \end{pmatrix} \right)$$

- The standard errors σ_{ji} depend on the **Fisher information** available
- For each arm j , **correlations** ρ_{pq} between parameters θ_{jp} and θ_{jq} are assumed to be known

Note that for many endpoints an asymptotic normal distribution for a transformation of the parameters of interest holds, e.g. the **log odds** for binary endpoints or the **log hazard** for survival endpoints

Multi-criteria decision analysis (MCDA)

Multi-criteria decision analysis (MCDA) is a structured approach for **decision making** that involve balancing multiple factors.

For each dose j , the **true MCDA score** is constructed as follows:

- A **factor-specific score** is constructed plugging θ_{ji} in a *partial value function* $u(x)$,

$$u(x) = \begin{cases} 0 & \\ \frac{x - \theta_i^L}{\theta_i^U - \theta_i^L} & \\ 1 & \end{cases} \quad \theta_i^L, \theta_i^U \text{ represent the maximum and minimum plausible values for the parameters}$$

- An aggregated **MCDA score** is constructed

$$MCDA_j = \sum_{i=1}^I \omega_i u(\theta_{ji}) \quad \sum_{i=1}^I \omega_i = 1$$

A trivial way to estimate the MCDA scores consists in using the MLEs $\hat{\theta}_{ji}^{IA}$ instead of the true parameters θ_{ji} , however the variability of the estimates is not taken into account.

Probabilistic MCDA

In order to account for the **variability in the parameters estimates**, we can work in a Bayesian framework, following this procedure:

- Non informative **prior distributions** are assigned to the parameters, namely θ_{ji}^{prior}
- Once data are observed **posterior distributions** θ_{ji}^{post} are obtained via Bayesian rule
- The MCDA score is found transforming θ_{ji}^{post} as follows

$$MCDA_j = \sum_{j=1}^J w_j u(\theta_{ji}^{post})$$

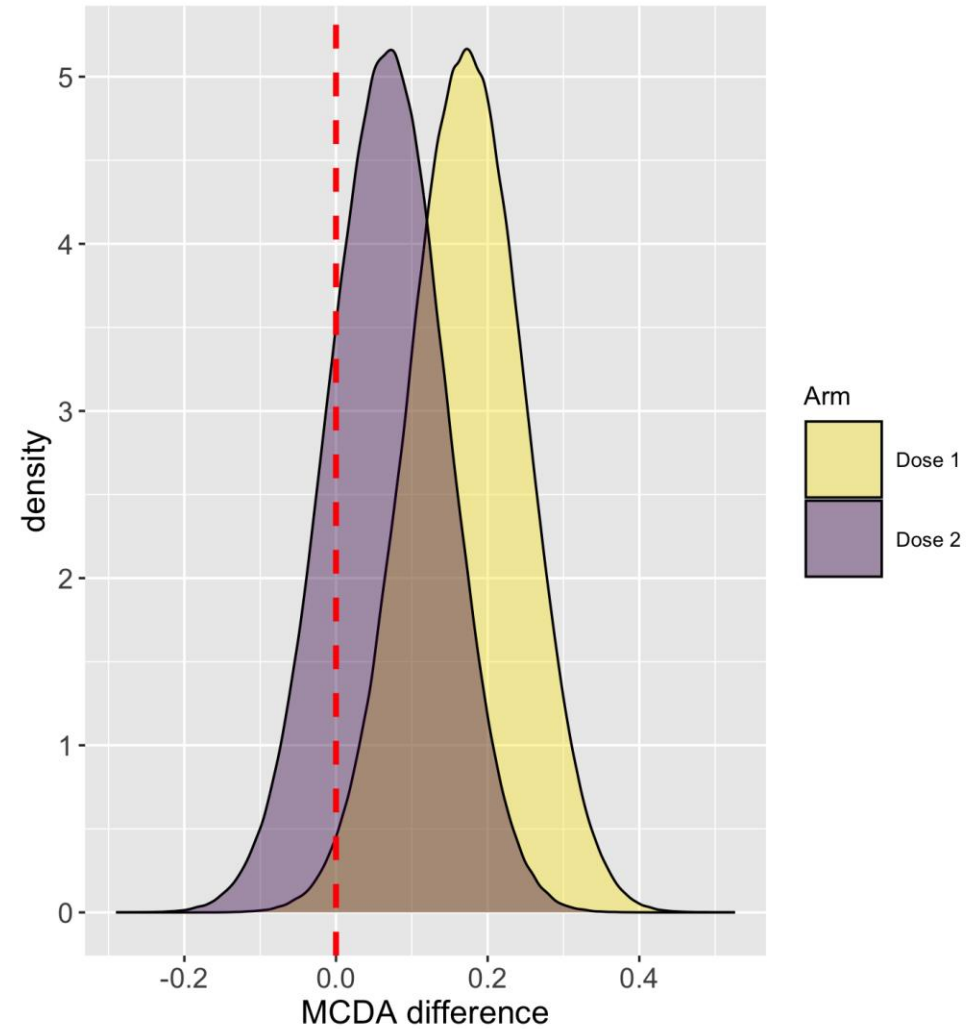
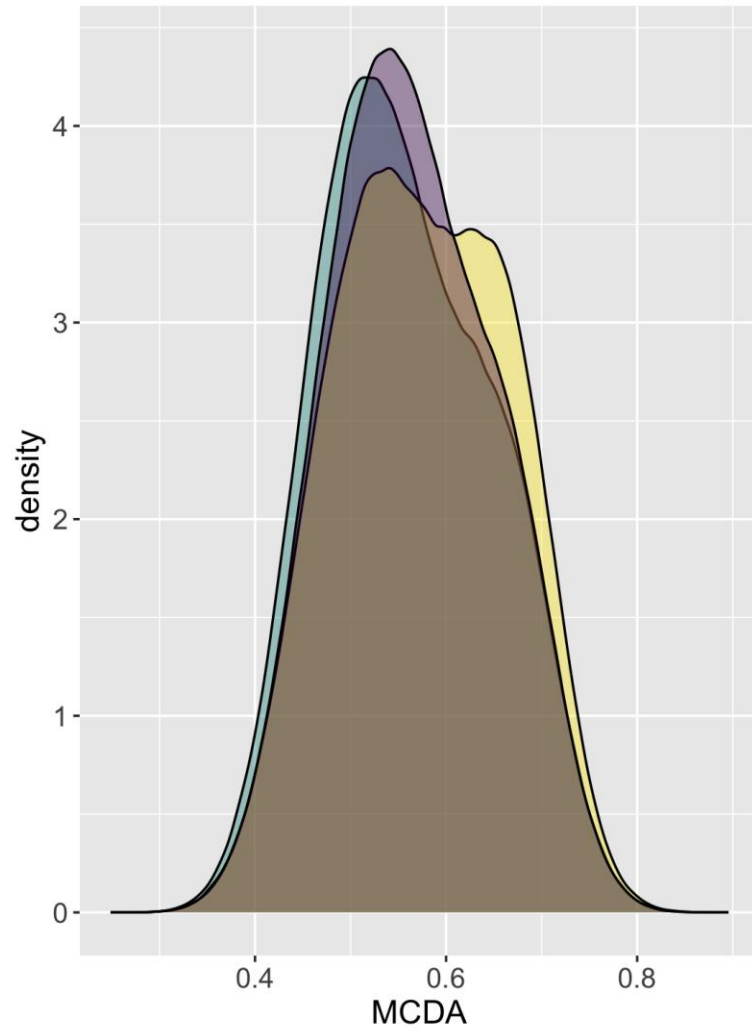
DOSE SELECTION RULE

- For each active dose, the posterior probability that its MCDA score is better than control is found and the dose with higher probability is selected

$$P_j = \mathbb{P}(MCDA_j > MCDA_0)$$

$$S = \operatorname{argmax}_{j=1, \dots, J} P_j$$

Visual representation of the selection rule



$$P_1 = 0.99$$
$$P_2 = 0.81$$



Dose 1 is selected

Distribution of the Z statistic (an idea..)

The interim test statistics Z_{S1}^{FA} can be written as

$$f_{Z_{S1}^{FA}}(x) = \sum_{j=1}^J \int_{-\infty}^{+\infty} f_{Z_{j1}^{FA} | Z_{j1}^{IA}}(z | Z_{j1}^{IA} = x) f_{Z_{j1}^{IA} | S}(x | S = j) f_S(j) dz$$

KEY ISSUE

The distribution of the selection random variable $S = \operatorname{argmax}_{j=1, \dots, J} P_j$, has no analytical form, because:

- It is based on a **probabilistic criterion** (based on Bayesian posterior probabilities)
- The posterior distribution of the MCDA scores is **discontinuous** due to the truncation introduced by the linear partial value function $u(\cdot)$

Approximation of the selection criterion

Hypothesis:

The upper and lower bounds of the linear partial value function $u(\cdot)$, namely θ_i^U and θ_i^L are chosen so that the posterior probability $P(\theta_i^L < \theta_i < \theta_i^U) \approx 1$

Equivalent selection rule:

An equivalence selection rule is:

$$S = \operatorname{argmax}_{j=1, \dots, J} \gamma_j$$

$$\gamma_j = \frac{\sum_{l=1}^I \omega_l [\prod_{k \neq i} (\theta_k^U - \theta_k^L)] (\hat{\theta}_{ji} - \hat{\theta}_{0i})}{\sqrt{\sum_{p,q} \rho_{pq} \omega_p \omega_q [\prod_{k \neq p} (\theta_k^U - \theta_k^L)] [\prod_{k \neq q} (\theta_k^U - \theta_k^L)] (\sigma_{jq} \sigma_{jp} + \sigma_{0q} \sigma_{0p})}}$$

- More **practical**, as does not need for Monte Carlo simulation
- An **analytical expression for the Z statistic** at final analysis can be derived

Strong control of type I Error control

Since the hypothesis testing at final analysis is **only on the primary endpoint**, the null hypothesis is

$$H_0: \theta_{01} = \theta_{11} = \theta_{21} = \dots = \theta_{I1}, \\ \theta_{ji} \in \mathbb{R}, \forall j, \forall i > 1$$

INFINITE MANY NULL CONFIGURATIONS!

HOW DO WE CHOOSE THE CONFIGURATION FOR TYPE I ERROR CONTROL ?

It can be proven that The distribution of Z_{S1}^{FA} is

- Stochastically increasing with $\delta_{ji}, \forall j, \forall i$
- Stochastically decreasing with $\sigma_{ji}^2, \forall j, \forall i$



Worst Case Configuration

$$\mathcal{C}: \theta_{ji} = \theta_{0i} = \operatorname{argmax}_{\theta_{ji}} \sigma_{ji}^2 \quad \forall j > 0, \forall i$$

Strong control of type I error is achieved if

$$\eta = \left| \operatorname{argmin}_q F(Z_{S1}^{FA} > q) - \alpha \right| \quad \text{under } \mathcal{C}$$

Power

Power is defined as the joint probability of these two events:

- Select a treatment which is effective on the primary endpoint
- Reject the null hypothesis for the selected treatment on the primary endpoint

However, as per the «null configurations», we have also **many alternative configurations**:

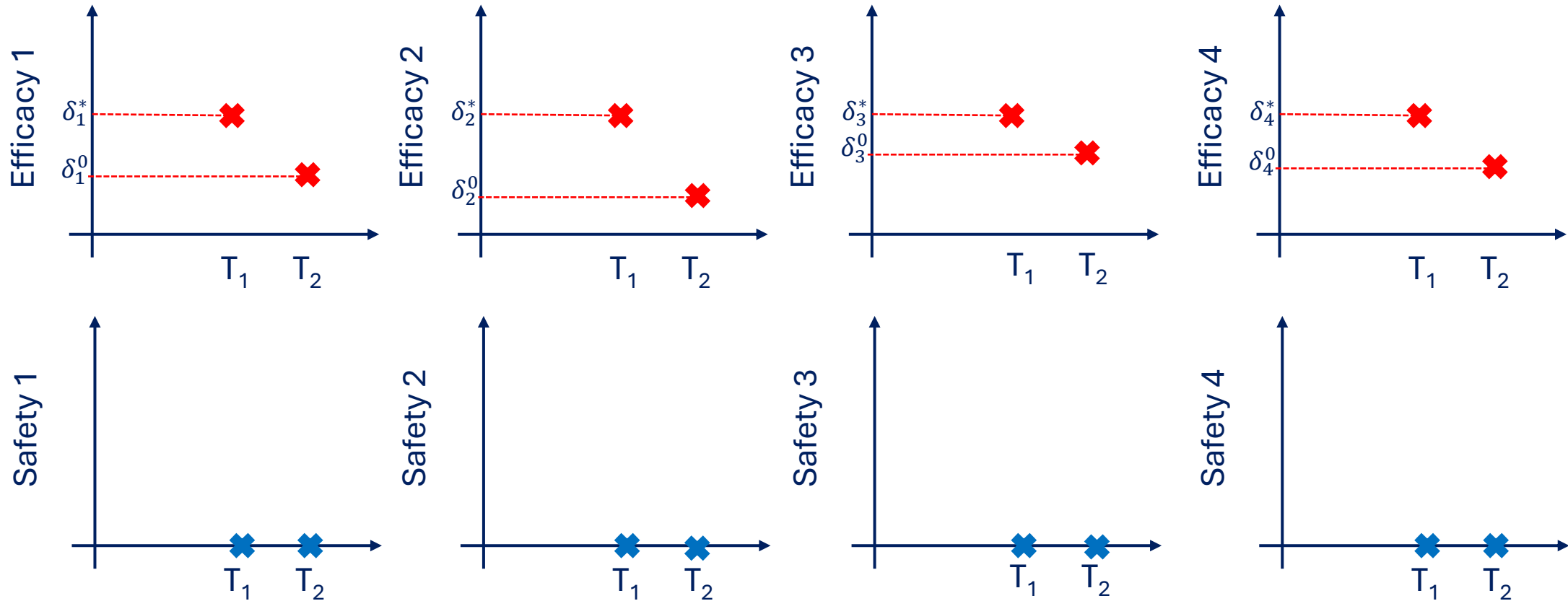
$$H_A: \theta_{j1} > \theta_{01} \text{ for at least one } j = 1, \dots, J$$
$$\theta_{ji} \in \mathbb{R}, \forall j, \forall i > 1$$

HOW DO WE CHOOSE THE CONFIGURATION FOR POWER ?

1. Assume that there exists **one single dose** which is superior in all efficacy endpoints at a level δ_i^*
2. Assume that the efficacy of all the other active doses is at the **maximum non relevant level** δ_i^0
3. All the doses are as safe as the control

**Least Favorable
Configuration**

Least Favorable Configuration (LFC)



The LFC represents the **best possible configuration** that the stakeholder would not be happy to select at the time of the interim analysis.

Sample Size determination

- Make some assumptions on the **control parameters** θ_{ji}
- Choose the **target treatment effects** on all efficacy endpoints, namely $\delta_1^*, \delta_2^*, \delta_3^*, \dots$
- Choose the **maximum non interesting treatment effects** on all efficacy endpoints, namely $\delta_1^0, \delta_2^0, \delta_3^0, \dots$
- Target the **information fraction of the interim analysis** on the primary endpoint (or expected information fraction if the timing is not driven by the primary endpoint)
- Target a **nominal level $1 - \beta$ for the rejection rate** under the Least Favorable Configuration (LFC)
- Find numerically the minimum sample size so that

$$F(Z_{S1}^{FA} > \eta) > 1 - \beta \quad \text{under LFC}$$

Design used in the simulations

- Two experimental doses, one common control arm
- 500 patients enrolled, with accrual rate 20 patients per arm per month
- Primary endpoint is OS
- For the MCDA we use:
 - Two efficacy endpoints: Overall Survival (OS) – primary endpoint
Overall Response Rate (ORR)
 - Two safety endpoints: Serious Adverse Events (SerAE)
Severe Adverse Events (SevAE)
- Weights $\omega = (0.1, 0.4, 0.25, 0.25)$ used in the probabilistic MCDA approach
- Interim Analysis after 183 patients overall are evaluable on ORR
- Final analysis after 179 OS events are observed across the selected arm and the control arm → 80% Power under the following Least Favorable Configuration (LFC)

LFC	Haz	ORR	SerAE	SevAE
Control	0.10	0.3	0.3	0.3
Dose 1	0.08	0.4	0.3	0.3
Dose 2	0.06	0.6	0.3	0.3

Stallard & Todd (2003) – competing approach

STATISTICS IN MEDICINE
Statist. Med. 2003; **22**:689–703 (DOI: 10.1002/sim.1362)

Sequential designs for phase III clinical trials incorporating treatment selection

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- The best performing treatment **on the primary endpoint** is selected
- Only primary endpoint is tested at the time of the final analysis
- Critical value η is computed in order to control type I error at the nominal level under the least favorable configuration (**expressed only in terms of primary endpoint**)

Operating characteristics used in the simulation study

- Probability that **dose 2 is selected** and continued until final analysis.
(dose 2 is always the «best dose» on the primary endpoint in the simulation setting)
- **Type I Error:** probability to reject the null hypothesis that the selected treatment is effective on the primary endpoint, when none of the active treatment is effective on the primary endpoint.
- **Power:** probability to jointly make the «right selection» and reject the null hypothesis for the selected treatment when the best treatment has a treatment effect of $HR(OS)=0.6$
- **Uninteresting Success:** probability to jointly make the «wrong selection» and reject the null hypothesis for the selected treatment when the best treatment has a treatment effect of $HR(OS)=0.6$
- **Average Toxicity:** average toxicity (on the probability scale) for the selected dose for each safety endpoint considered

Type I Error analysis

- Dose 1 is equivalent to control
- Varying characteristics of dose 2
- Selection based on probabilistic MCDA.
- FA after **174 OS events**, IF after **183 patients on ORR**.

Characteristics of dose 2

	Haz	ORR	Tox 1	Tox 2
S1	0.1	0.3	0.3	0.3
S2	0.1	0.5	0.3	0.3
S3	0.1	0.7	0.3	0.3
S4	0.1	0.3	0.45	0.4
S5	0.1	0.7	0.6	0.5

	γ_1	γ_2	Our Approach		Stallard & Todd	
			P(sel. T2)	t1e	P(sel. T2)	t1e
S1	0	0	50.3	2.2	50.2	2.2
S2	0	1.56	94.1	2.2	49.6	2.5
S3	0	3.14	99.9	2.0	48.7	2.5
S4	0	-1.25	10.6	2.2	50.7	2.4
S5	0	0.74	76.5	2.3	50.2	2.5

- Type I Error is strictly controlled below 2.5%, while it is controlled exactly at 2.5% for Stallard & Todd
- Probability of selecting dose 2 depends on $\gamma_2 - \gamma_1$

Power analysis

- FA after **179 events** are observed (control + selected arm)
- IA after **183 responses** on secondary efficacy endpoint
- Almost **20% IF** on primary endpoint

Characteristics of control arm

Haz	ORR	Tox1	Tox2
0.1	0.3	0.3	0.3

Characteristics of dose 1

Haz	ORR	Tox1	Tox2	MCDA
0.08	0.4	0.3	0.3	1.23

Characteristics of dose 2

					Our Approach					Stallard & Todd				
Haz	ORR	Tox1	Tox2	γ_2	Avg Tox 1	Avg Tox 2	Sel T2	Unint. Success	Pow	Avg Tox 1	Avg Tox 2	Sel T2	Unint. Success	Pow
0.06	0.6	0.3	0.3	2.83	0.30	0.30	95.9	1.7	79.2	0.30	0.30	67.9	11.7	57.7
0.06	0.7	0.3	0.3	3.64	0.30	0.30	99.4	0.2	82.2	0.30	0.30	67.7	12.2	57.4
0.06	0.6	0.5	0.5	0.92	0.38	0.38	39.2	20.9	33.5	0.44	0.44	66.9	12.5	57.3
0.06	0.7	0.55	0.55	1.29	0.44	0.44	54.5	15.9	46.5	0.48	0.48	68.3	12.2	57.9
0.06	0.3	0.4	0.4	-0.5	0.31	0.31	16.6	30.7	3.5	0.37	0.37	68.1	11.8	57.9

- ✓ Power may be lower or higher wrt Stallard & Todd depending on the benefit-risk profile
- ✓ Arms with high level of toxicity are recommended less on average with our approach

Summary

- We constructed a seamless phase 2/3 design where:
 - Selection at IA is based on **probabilistic linear MCDA**
 - Final hypothesis testing is based on **primary endpoint**

- An **analytical expression** for the distribution of the test statistic at the final analysis is not available, but can be approximated under reasonable assumptions

- **Strong control of type I error** at the nominal level α is achieved computing the critical value of the final test under a «worst case configuration»

- Results show that including MCDA in the selection step of the design effectively helps in **limiting the probability to select potentially toxic doses**, still achieving good power if the most effective dose has also exhibits a good benefit-risk profile

Thank you for the attention!