



PSI Conference

# *A Comprehensive Self-Adaptive Mixture Prior Approach to Dynamic Borrowing from External Data*



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Statistical Innovation  
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# Outline

- // Introduction
- // Bayesian Dynamic Borrowing from External Data
- // Propensity Score Integrated Self Adaptive Mixture Prior (PSI-SAMP)
- // Simulation Results
- // Illustrative Example
- // Summary and Conclusions



# *Introduction*

**Motivation and challenges**



# Introduction

Motivation and challenges in leveraging external data for the analysis of RCTs

## Randomized Control Trials (RCTs)

- Considered the “gold standard” to evaluate efficacy and safety of treatments
- Randomization aims to **balance** observed covariates across treatments
- Randomization not always feasible (recruitment, ethical, duration, costs, etc.)

## External Data Sources (e.g., historical trials, RWD)

- Issues to be considered when using external data:
  - The **similarity** between trial patients and those from external data sources
  - The **amount of information** that the external data contributes to the statistical inference

## Our Goal

- Develop a comprehensive, **self-adaptive** Bayesian dynamic borrowing approach that adjust for both **baseline** and **outcome** differences to determine the **amount of information** borrowing



# *Bayesian Dynamic Borrowing from External Data*

**A Brief Review**



# Power Prior Approach

Ibrahim and Chen (2000), Ibrahim et al (2015), Neuenschwander et al (2009)

// Bayesian inference of parameter  $\theta$ , given current data  $D_1$  and external data  $D_0$  is through the following expression:

$$\pi(\theta|D_1) \propto \underbrace{L(D_1|\theta)}_{\text{Likelihood}} \underbrace{L(D_0|\theta)^{\alpha_0}}_{\text{Power prior}} \underbrace{\pi_0(\theta)}_{\text{Initial prior}}$$

Posterior

Idea: construct informative prior from historical data; define power parameter to down-weight the influence of historical data on the analysis

- $L(D_1|\theta)$  is the likelihood of the **current data** given parameter  $\theta$
- $L(D_0|\theta)$  is the likelihood of **external data** given parameter  $\theta$
- $0 \leq \alpha_0 \leq 1$  is a scalar parameter (fixed or random) that controls the weight of influence of  $D_0$  in the analysis of  $D_1$ ; with higher values of  $\alpha_0$ , more information is borrowed from  $D_0$
- $\pi_0(\theta)$  is an initial prior



# Propensity Score-Integrated Power Prior (PSIPP)

Wang et al (2019): Adjusts borrowing based on stratified propensity score (PS) similarity

// Stratify current and external subjects into S strata (PS percentiles)

Idea: use overlap of stratified PS distributions of current and external patients to down-weight the external data in the analysis

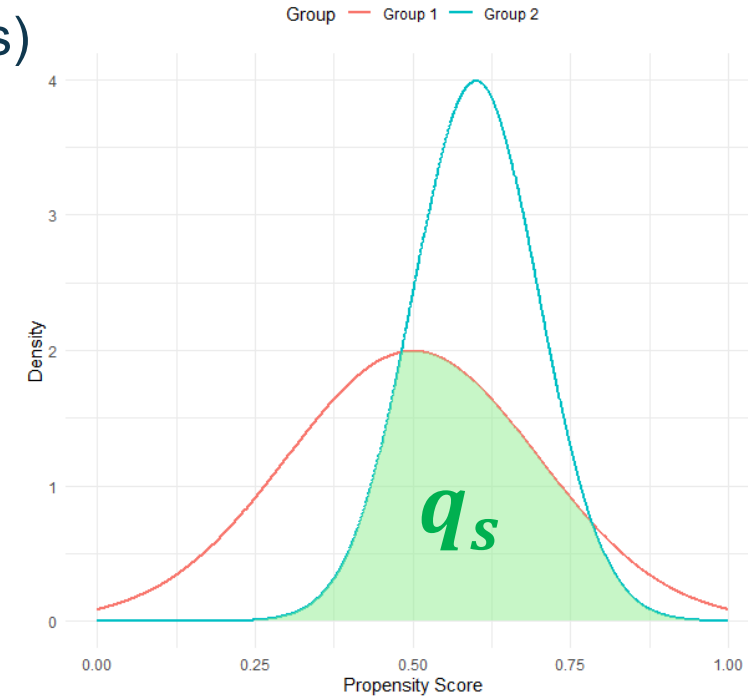
//  $q_s$ : overlapping area of PS distributions of current and external patients

//  $A$ : number of subjects to borrow

//  $n_{0,s}$ : number of external subjects in strata s

// Discount power parameter:  $\alpha_s = \min\left(1, \frac{A}{n_{0,s}} \frac{q_s}{\sum_{i=1}^S q_s}\right)$

// **Power prior:**  $\pi(\theta_1, \dots, \theta_s) \propto \prod_{s=1}^S [L(D_{s,0}|\theta_s)]^{\alpha_s} \pi_0(\theta_1, \dots, \theta_s)$



$$q_s = \int_0^1 \min[p_{s,0}(x), p_{s,1}(x)] dx$$



# Mixture Prior Approach

Schmidli et al. (2014)

To account for the possibility of prior-data conflict and improve the robustness of the inference, fixed-weight mixture prior have been proposed:

$$\pi_{mixture}(\theta) = \tilde{\omega}\pi_{informative}(\theta) + (1 - \tilde{\omega})\pi_{vague}(\theta)$$

Idea: combine and informative prior with a non-informative or vague prior into a single distribution, through a mixing weight

$\pi_{informative}(\theta)$ : Informative prior constructed from external data

$\pi_{vague}(\theta)$ : Non-informative or vague prior

$\tilde{\omega}$ : **prespecified fixed** mixing weight (representing the prior probability of no prior-data conflict between  $D_1$ (current) and  $D_0$ (external))



# *Propensity Score Integrated Self Adaptive Mixture Prior*

**A comprehensive  
integrated method**

# Proposed Self-Adaptive Mixture Prior Approach

Define self-adaptive mixture weight

// Assess similarity between current and external data via the **predictive probability of observing the current data given the external data** via the Posterior Predictive Probability:

$$PPP = \Pr(\tilde{\mu}_1 > \bar{y}_1 | y_0)$$

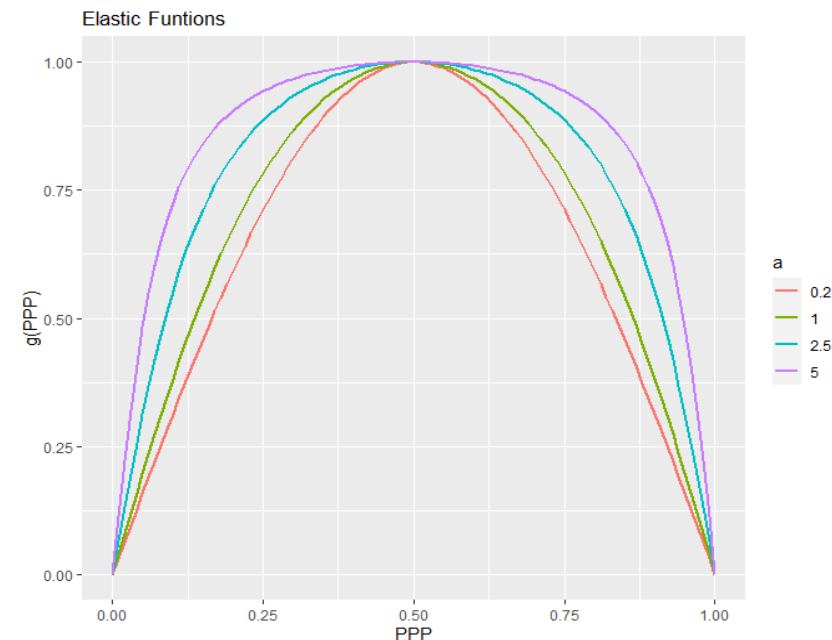
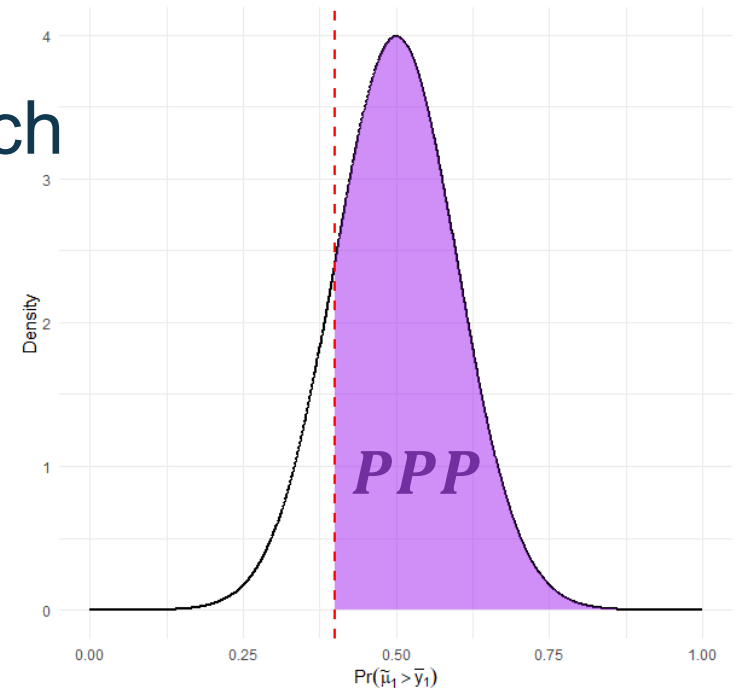
- $\tilde{\mu}_1$  is the predictive sample mean given external data  $y_0$
- $\bar{y}_1$  is the sample mean of the current data

// If external and current data are similar,  $PPP \approx 1/2$

// Elastic function  $g(PPP) = \frac{\arctan(a \times \sin(PPP * \pi))}{\arctan(a)}$

// The value of  $a$  can be tuned with clinical input

Self-adaptive mixture weight:  $\omega = g(PPP)$





# Proposed Self-Adaptive Mixture Prior Approach

The self-adaptive mixture prior for stratum  $s = 1, 2, 3 \dots, S$ , is given by:

$$\pi_{SAMP,s}(\theta) = \omega_s(\mathbf{PPP}_s)\pi_{informative,s}(\theta) + [1 - \omega_s(\mathbf{PPP}_s)]\pi_{vague,s}(\theta)$$

$\pi_{informative,s}(\theta)$ : Informative prior for stratum  $s$  (derived via PSIPP)

$\pi_{vague,s}(\theta)$ : Non-informative or vague prior for stratum  $s$

$\omega_s(\mathbf{PPP}_s)$ : Self-adaptive mixture weight for stratum  $s$  (depends on PPPs through the elastic function  $g(*)$ )



# *Simulation Results*

## **Binary Outcomes**



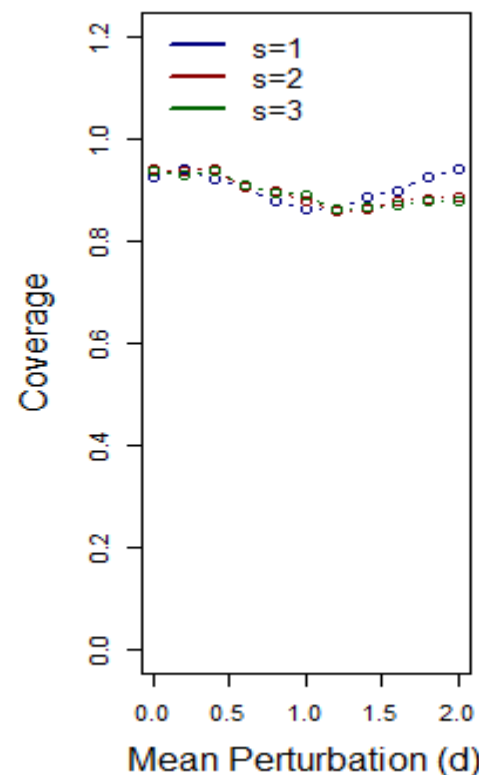
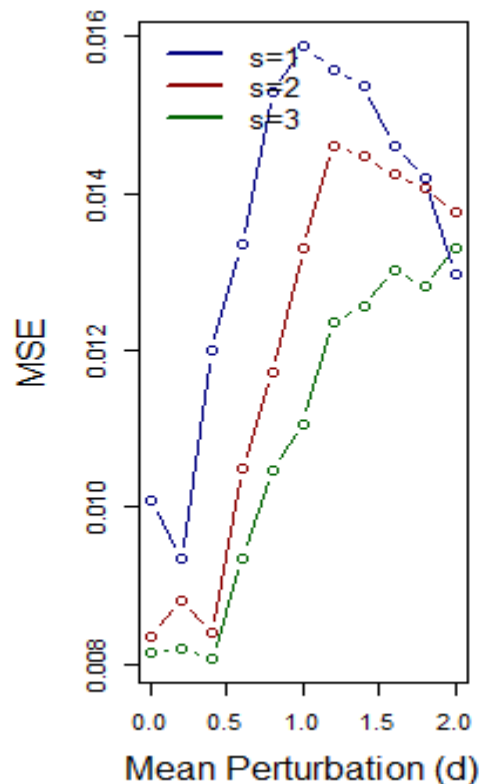
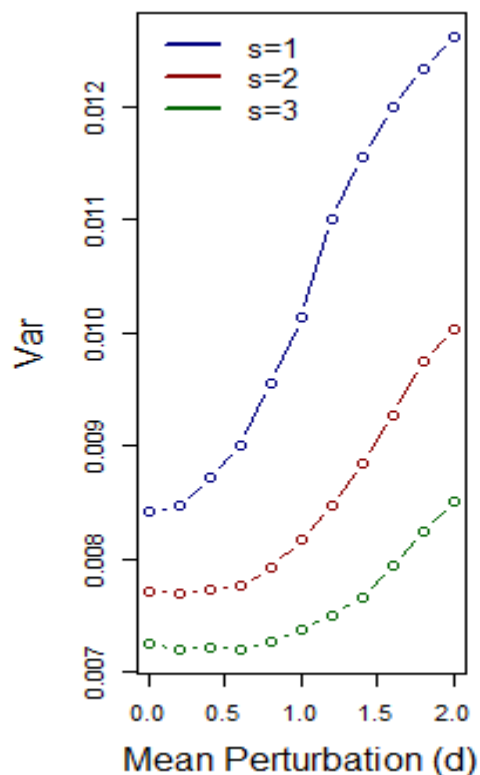
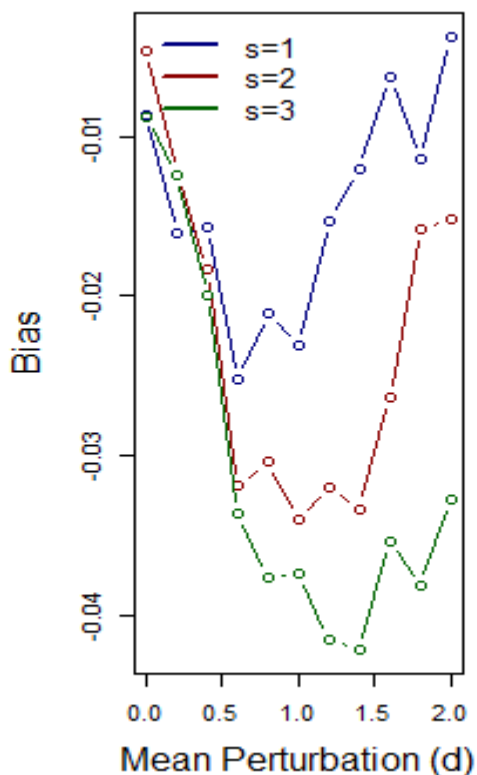
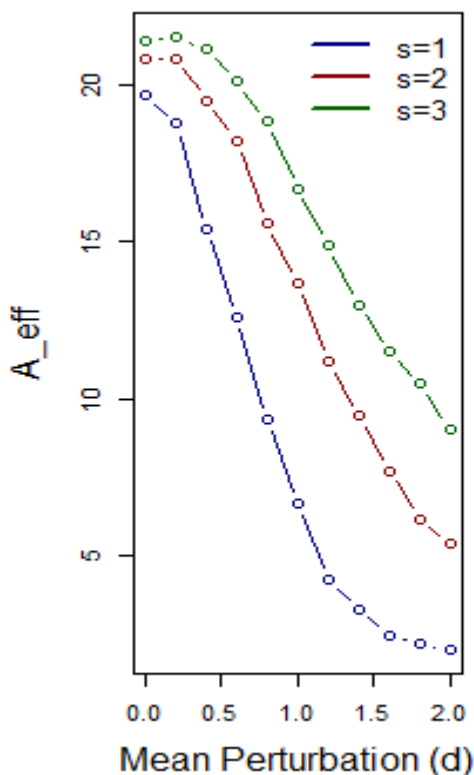
# Binary Outcome – Hybrid Control Arm

N1=75 (current), 2:1 treatment-to-control, A=25 (no. to borrow), N0=3000 (external), and s=3 (strata)

$$\text{logit}(Y_i|X_i, Z_i) = \beta_0 + \boldsymbol{\beta}^T X_i + O_i; \mathbf{X} = (X_1, \dots, X_{10})^T; \beta_0 = -10.48; \boldsymbol{\beta} = (1, \dots, 1)^T; F_{X|Z} = \text{MVN}(\mu_Z, \Sigma_Z)$$

$$Z = 1 \text{ (current)} \quad \mu_1 = (1, \dots, 1)^T \quad \sigma_1^2 = 0.1 \quad O_1 = 0$$

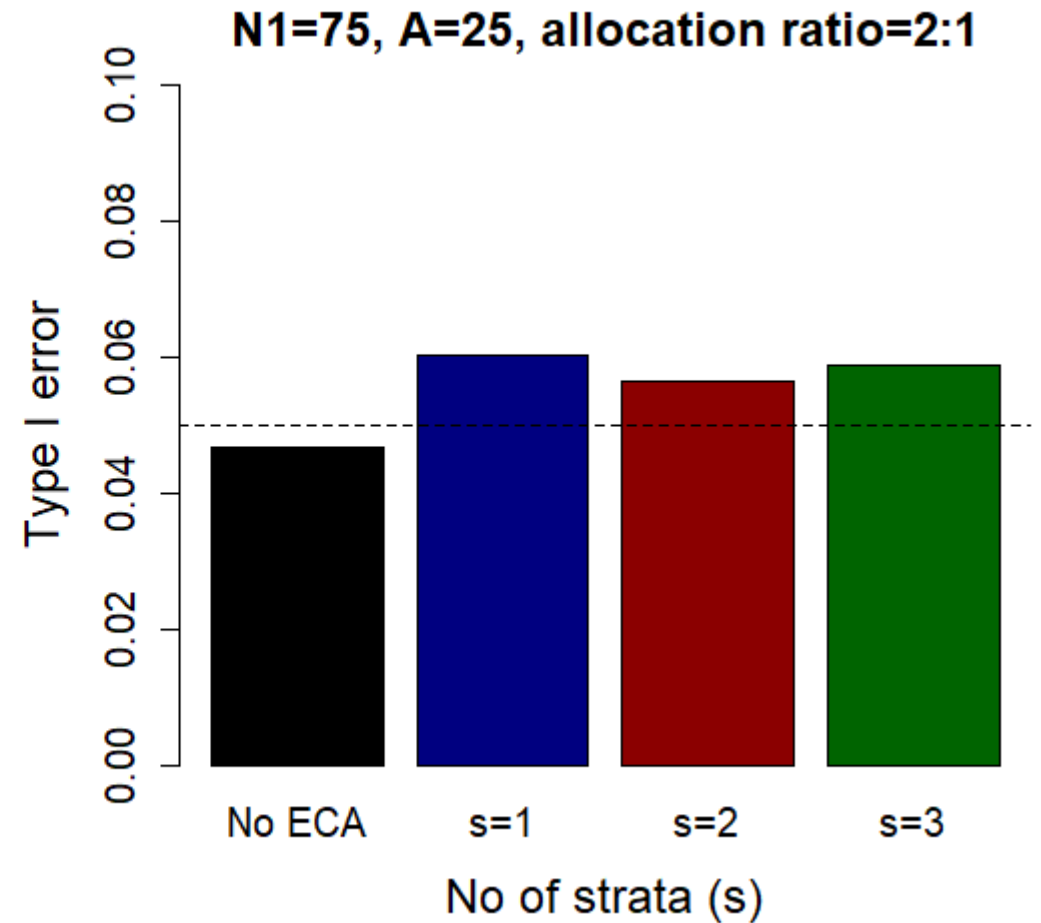
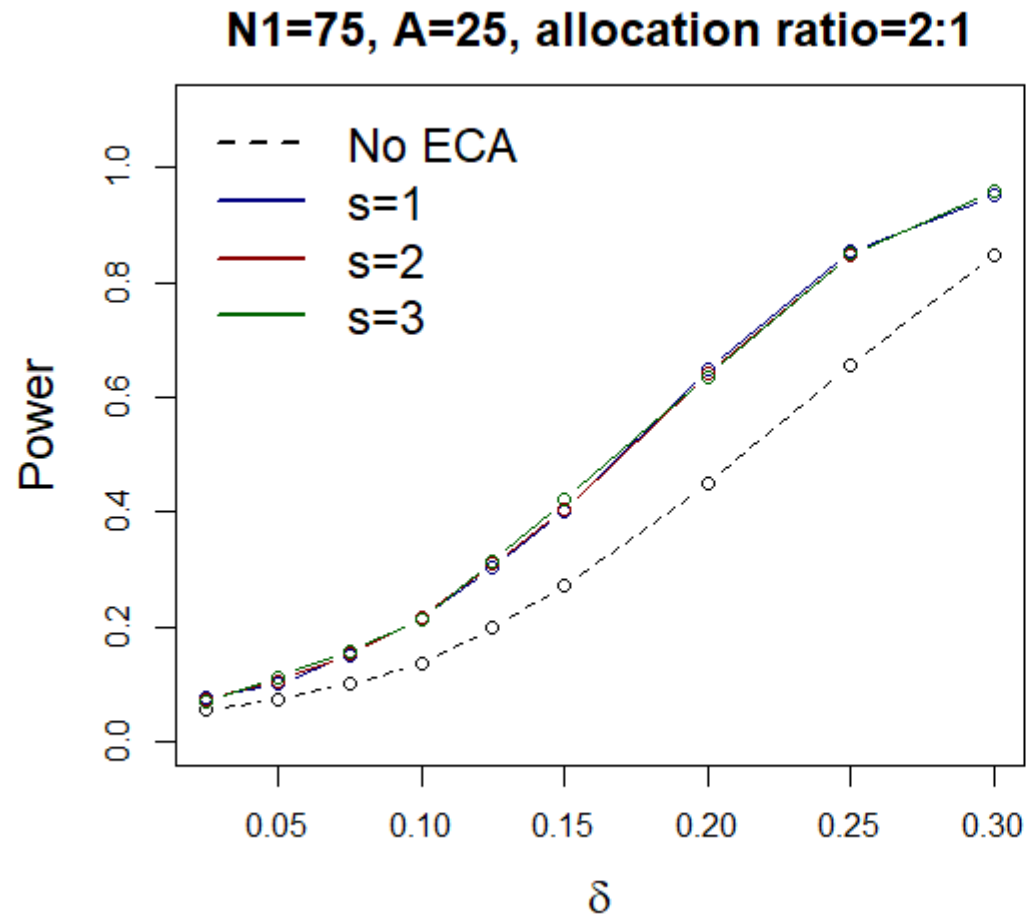
$$Z = 0 \text{ (external)} \quad \mu_0 = (1.02, \dots, 1.02)^T \quad \sigma_0^2 = 0.12 \quad O_0 \sim N(d, 0.25) \text{ (random perturbation)}$$





# Binary Outcome – Hybrid Control Arm

$N_1=75$  (current), 2:1 treatment-to-control,  $A=25$  (no. to borrow),  $N_0=3000$  (external), and  $s=3$  (strata)





# *Illustrative Example*

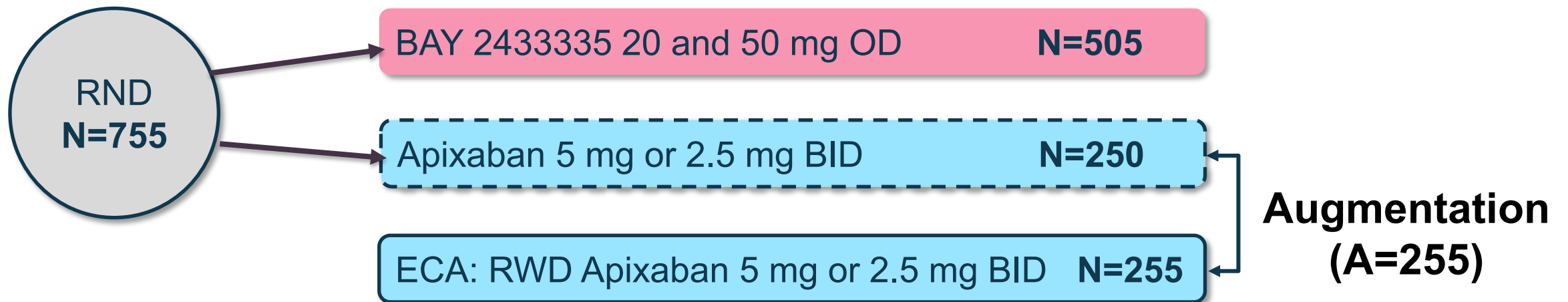
**Addressing both baseline  
and outcome differences**



# Illustrative Example

PACIFIC-AF Phase II trial and External RWD

- // **Trial data:** Phase II trial (PACIFIC-AF) to compare efficacy and safety of new factor Xla inhibitor against Apixaban. Two active dose groups and control arm (**N=755,  $\approx$  2:1 ratio**)
- // **External data:** RWD with identical selection criteria as in the trial (N=3327)
- // **Outcome:** Major bleeding within 90-days
- // **Key Idea:** Augment control arm by borrowing information **equivalent to 255** patients from RWD to attain 1:1 ratio of treatment to control

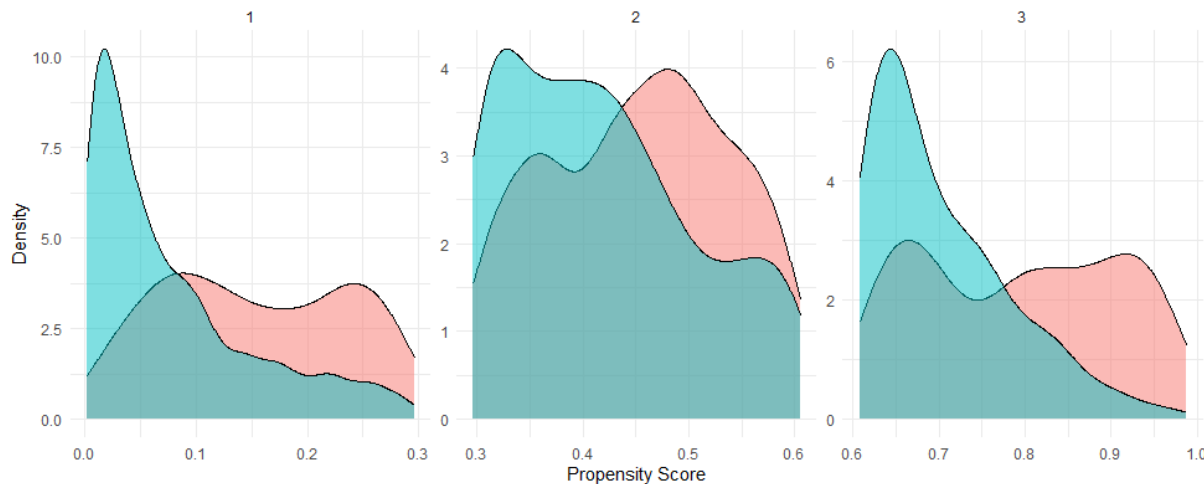




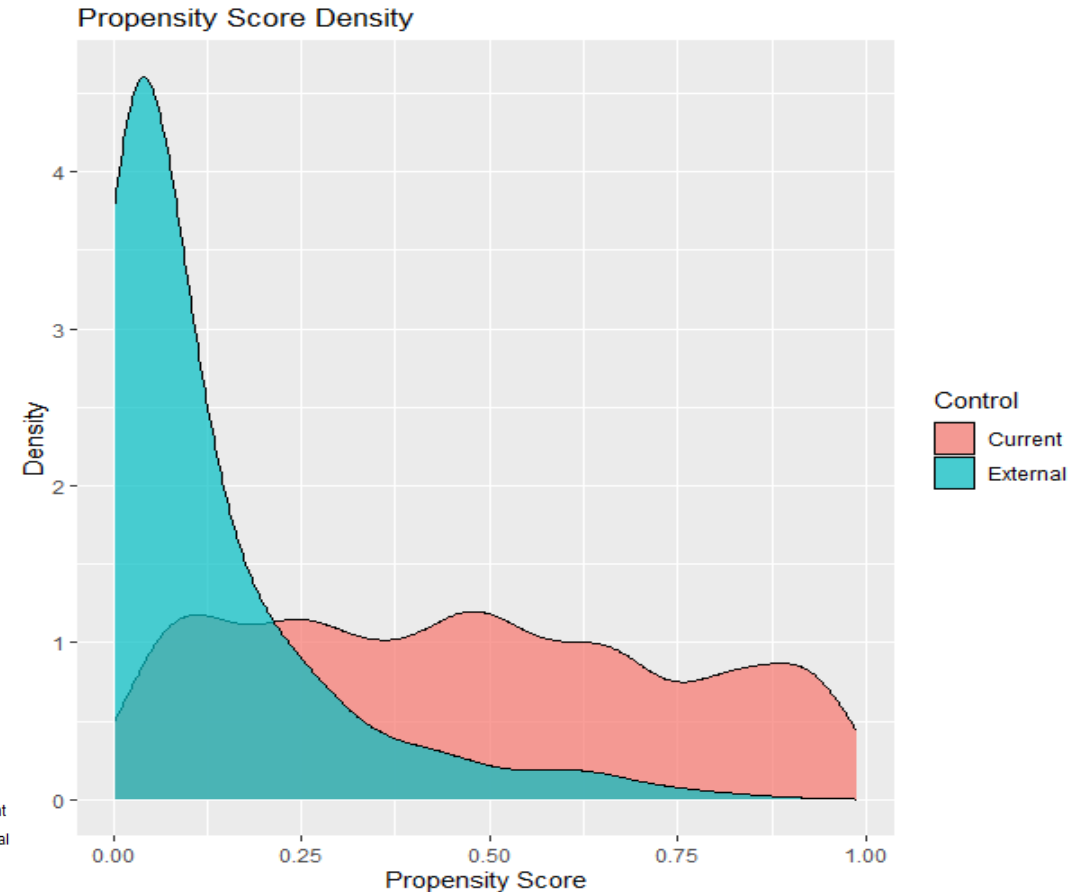
# PS Modeling, Estimation, Trimming

Similarity of baseline data – current vs. external control

- // Propensity scores estimated via logistic regression (trial: 755, RWD: 3327)
- // 33 baseline covariates as additive linear terms
- // Trimming: 3204 of the 3327 external patients were retained (123 excluded)
- // Number of strata **s=3**



**Figure.** Propensity score densities by stratum



**Figure.** Propensity score densities for the current study and external data for the illustrative example.



# Summary of Current and External Data

PACIFIC-AF Phase II trial and External RWD

Parameter		Stratum			Total
		$s = 1$	$s = 2$	$s = 3$	
<b><u>Current Study (sample size)</u></b>	$n_{s1}$	252	251	252	755
<b>Treatment</b>	$n_{s11}$	172	172	161	505
<b>Control</b>	$n_{s10}$	80	79	91	250
<b><u>Current Study (no. of events)</u></b>					
<b>Treatment</b>	$ne_{s11}$	1	1	2	4
<b>Control</b>	$ne_{s10}$	2	1	3	6
<b>External data (sample size)</b>	$n_{s0}$	2823	294	87	3204
<b>External data (no. of events)</b>	$ne_{s0}$	86	8	1	95



# Parameters of the self-adaptive mixture prior approach

PACIFIC-AF Phase II trial and External RWD

Parameter		Stratum*			Total
		$s = 1$	$s = 2$	$s = 3$	
Overlapping coefficient	$q_s$	0.62	0.82	0.64	
Overlapping coefficient normalized	$v_s$	30%	39%	31%	100%
Discount power parameter	$\alpha_s$	0.027	0.341	0.904	
Posterior Predictive Probability	$PPP_s$	0.451	0.626	0.129	
Self-adaptive mixture weight ( $a = 0.1$ )*	$\omega_s$	0.988	0.923	0.395	
Effective sample size	$A_{eff}$	77	96	48	<b>221</b>

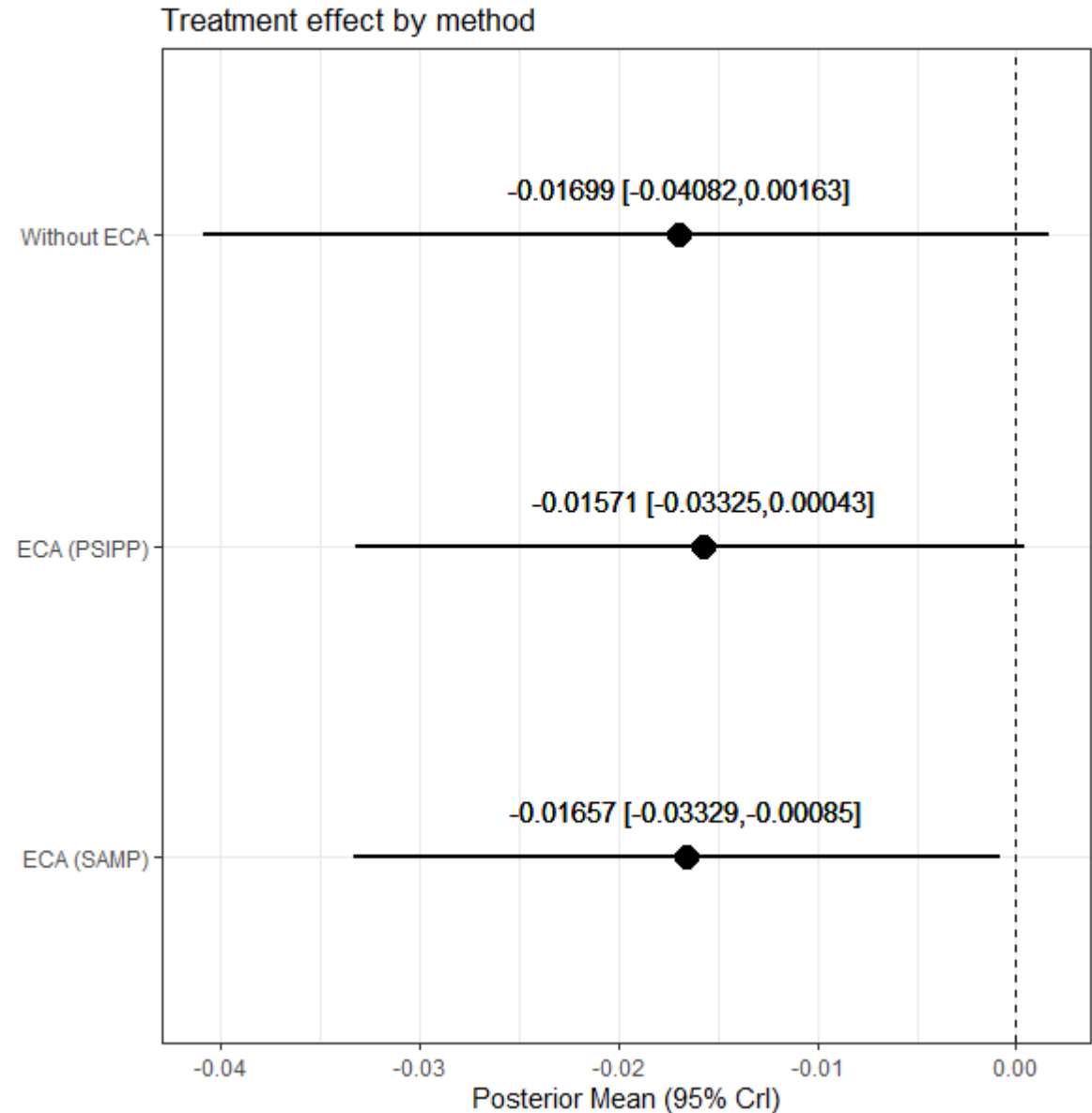
\* Number of strata (s) and tuning parameter (a) can be chosen through a grid search aimed at minimizing the MSE



# Comparison of Analyses

PACIFIC-AF Phase II trial and External RWD

- // Bayesian analysis:
  - // Without ECA (Trial data)
  - // With ECA (PSIPP)
  - // With ECA (PSI-SAMP)
- // Adjusting for baseline only, increases precision but slightly shifts the estimate
- // Analysis adjusting for baseline & outcome differences attenuates the bias resulted from borrowing from the ECA





# *Discussion*

## **Summary and Conclusions**



# Summary and Conclusions

- // We propose an integrated self-adaptive Bayesian dynamic borrowing approach
- // Baseline differences are accounted for by the overlap of the stratified propensity score distributions
- // Self-adaptive mixture weights are function of the predictive posterior probability of observing the current outcome given the outcome of the external data
- // The target number of external subjects  $A$  is discounted according to the observed degree of difference between current and external data
- // Simulations show desirable operating characteristics and adaptive information borrowing
- // The proposed approach is intuitive, allows flexibility for adjusting the amount of borrowing, and it enables the incorporation of expert opinion



# Key References

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*Thank you!*



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# *Back up*

# Elastic Prior Approach

Jiang et al (2021)

- // **Key idea:** Use of “congruence measure” (e.g. T-test) to assess similarity of current  $D_1$  and external data  $D_0$ .
- // An “elastic function”  $g(T)$  is used to map the congruence measure to the interval (0,1)
- // The mapped value is used to adjust the prior variance, controlling how much the external data influences the analysis

// Example: Normal endpoint

- //  $y_{1,i} \sim N(\theta, \sigma^2)$ ,  $y_{0,i} \sim N(\theta_0, \sigma_0^2)$ , with interest in estimating  $\theta$
- // Assuming that  $D_1$  and  $D_0$  are incongruent

// **Elastic prior:**  $\pi^*(\theta|D_0) = N\left(\bar{y}_0, \frac{\sigma_0^2}{n_0 g(T)}\right)$

**variance is inflated with the elastic function  $g(T)$**

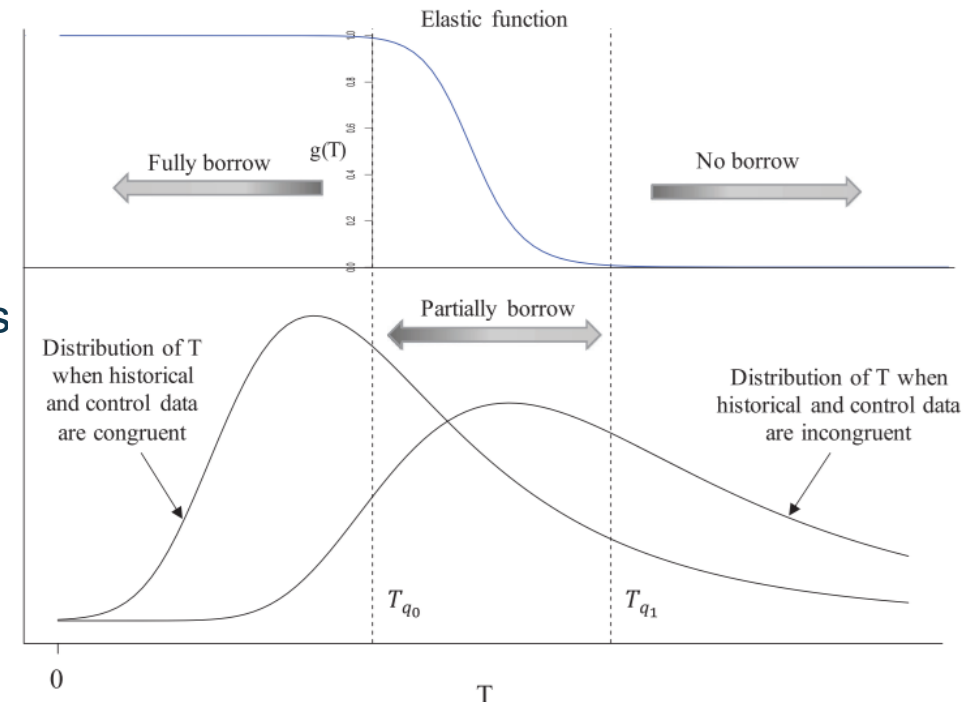


Figure (Jiang et al 2021). Dynamic information borrowing through elastic function

# How to choose tuning parameter (a) and number of strata (s)?

Practical recommendations for user-specified parameters

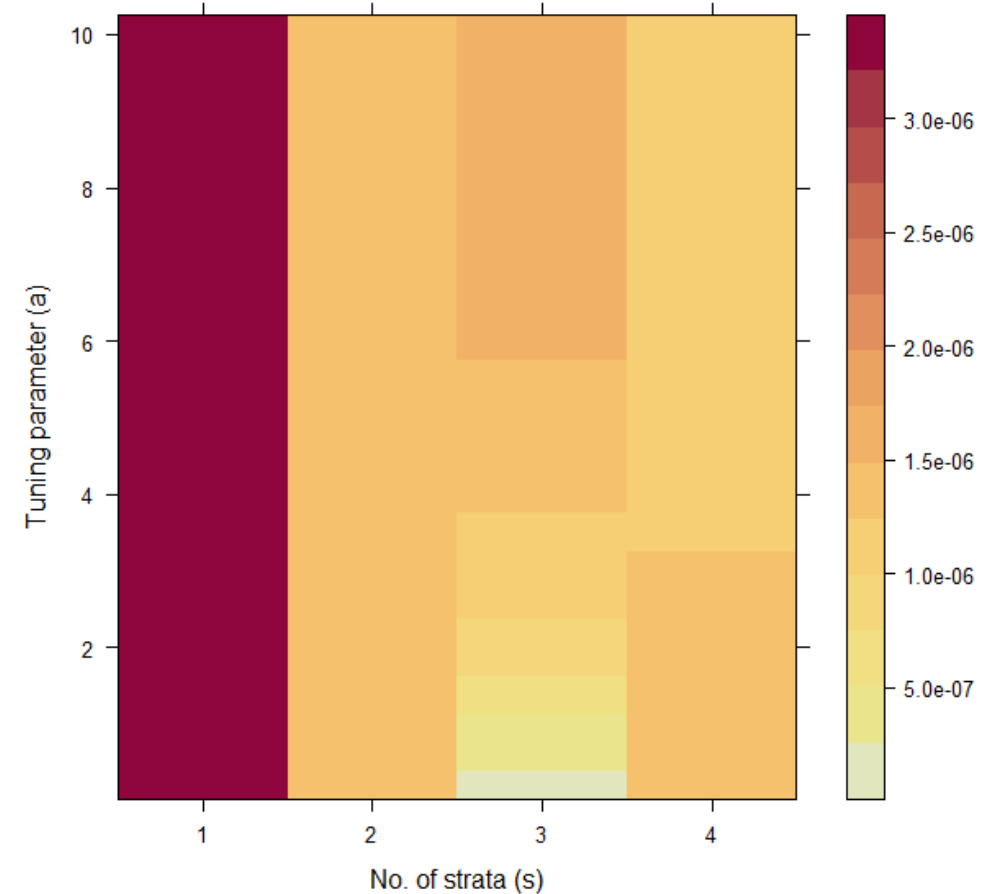
1) Use as reference  $\theta_T$  (treatment effect from current trial)

2) Define:

$$MSE(s, a) = (\hat{\theta}(s, a) - \theta_T)^2 + Var(\hat{\theta}(s, a))$$

where  $\hat{\theta}(s, a)$  is the double adjustment estimator

3) Do a grid search over parameters a and s to minimize MSE



Heatmap of mean squared error  $MSE(s, a)$ . Minimum is attained at  $a=0.1$  and  $s=3$



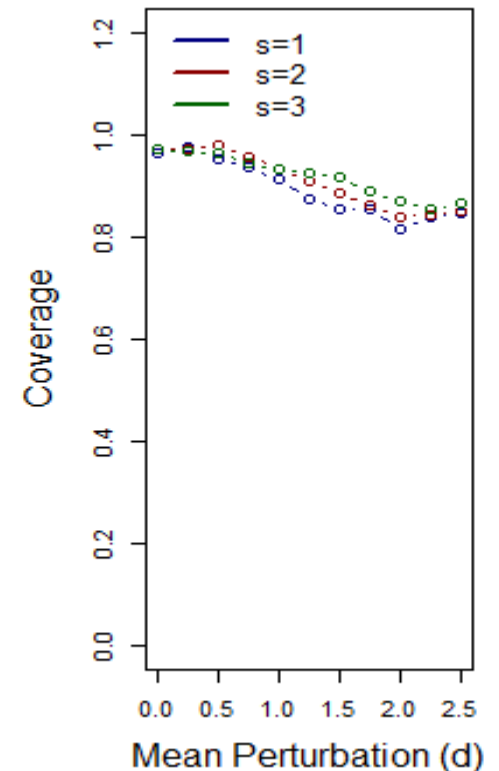
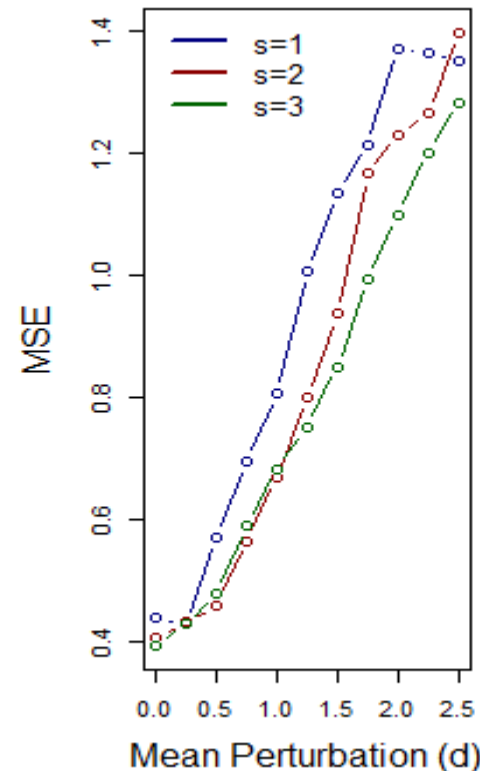
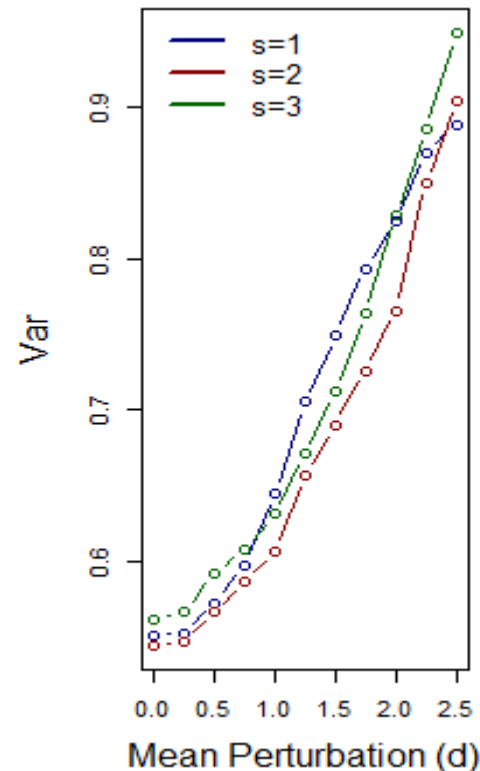
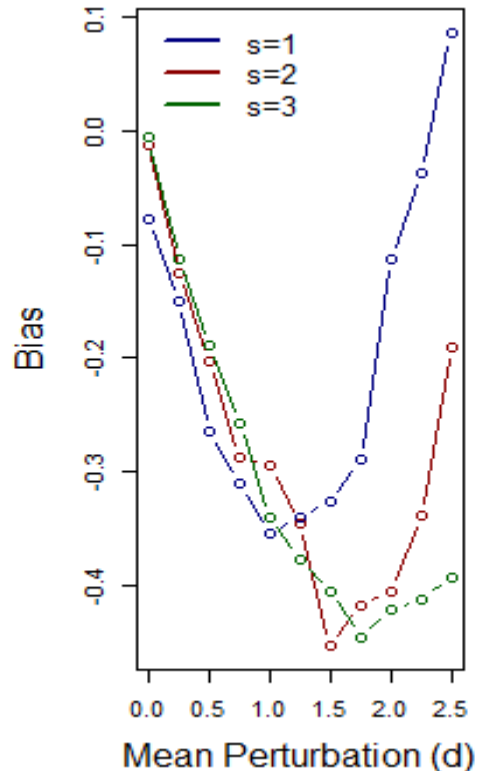
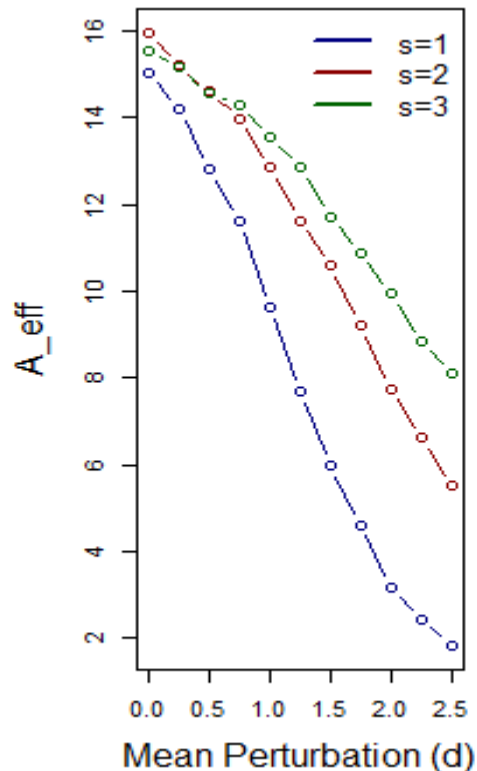
# Continuous Outcome – Hybrid Control Arm

Effective SS, bias, variance, MSE and coverage for  $N_1=75$  (current),  $N_0=3000$  (external), and  $s=3$  (strata)

$$Y_i|X_i, Z_i = \beta_0 + \boldsymbol{\beta}^T X_i + \epsilon_i + O_i; \mathbf{X} = (X_1, \dots, X_{10})^T; \beta_0 = 0; \boldsymbol{\beta} = (1, \dots, 1)^T; \epsilon_i \sim N(0, 1); F_{X|Z} = MVN(\mu_z, \Sigma_z)$$

$$Z = 1 \text{ (current)} \quad \mu_1 = (1, \dots, 1)^T; \quad \sigma_1^2 = 1; \quad O_1 = 0$$

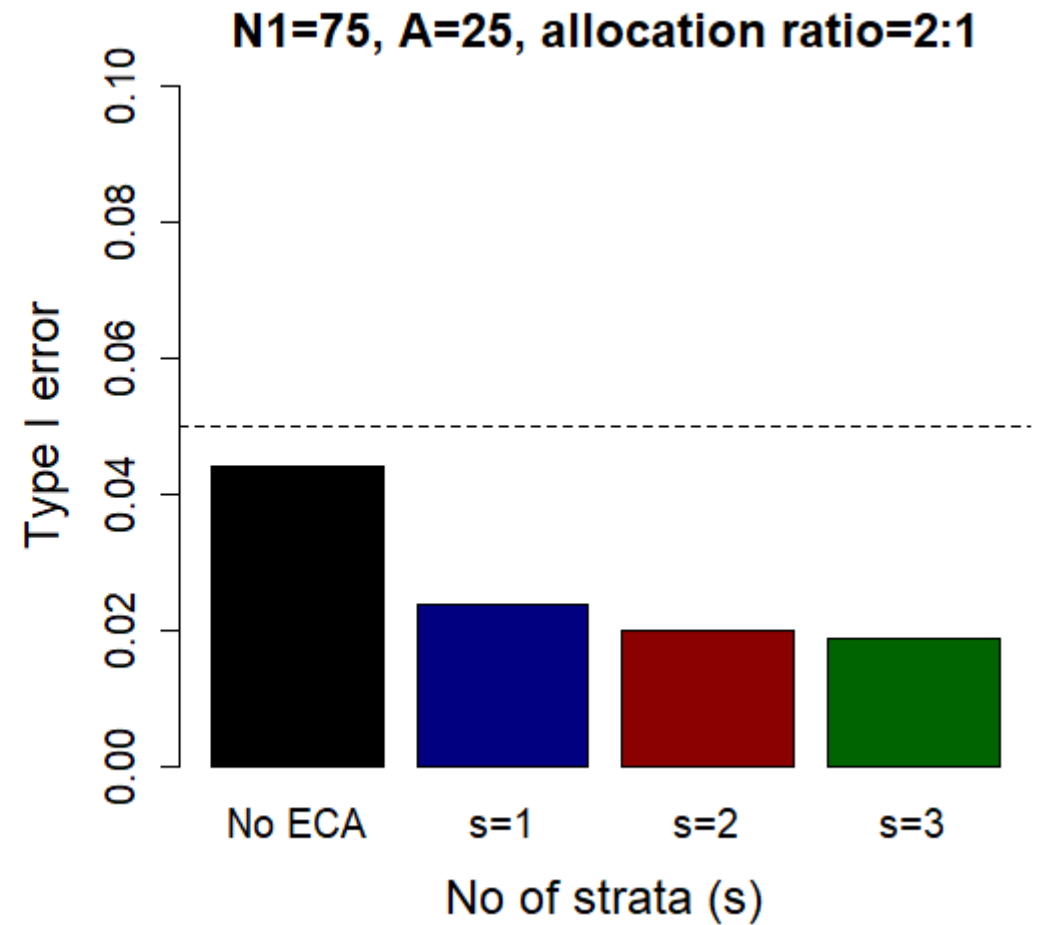
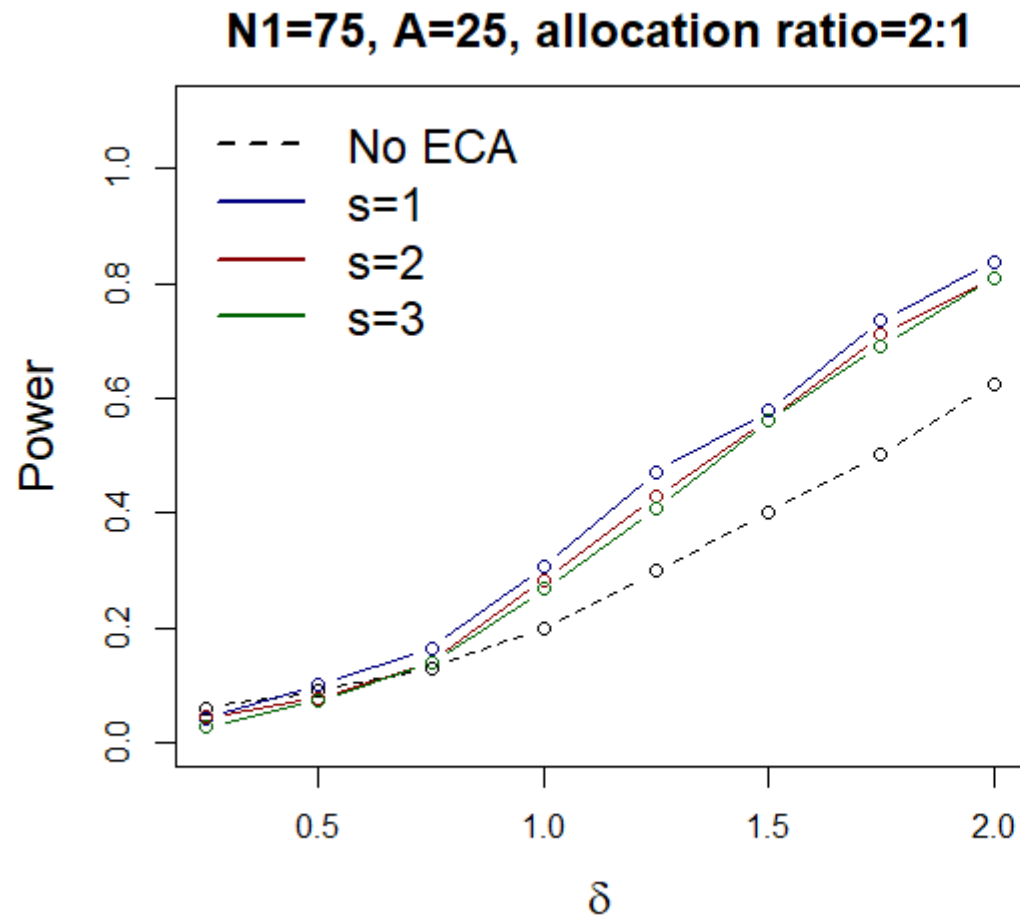
$$Z = 0 \text{ (external)} \quad \mu_0 = (1.05, \dots, 1.05)^T; \quad \sigma_0^2 = 1.5; \quad O_0 \sim N(d, 1.5) \text{ (random perturbation)}$$





# Continuous Outcome – Hybrid Control Arm

Power and Type I error,  $N_1=75$ ,  $N_0=3000$ , treatment-to-control allocation ratio 2:1,  $A=25$ ,  $s=3$





# Event Rates and Treatment Effect Estimates by Stratum

PACIFIC-AF Phase II trial and External RWD

